

## Weird Chemist

### de-Broglie Equation — DPP-7 Solutions

Chapter: Structure of Atom

“ $\lambda = h/mv$  — yeh ek formula hai. Iska sab kuch units pe depend karta hai. Convert karo, phir plug karo.”

#### Master Formulae — de-Broglie Equation

- $\lambda = \frac{h}{mv} = \frac{h}{p}$  (basic form)
- $\lambda = \frac{h}{\sqrt{2m \cdot KE}}$  (from  $KE = p^2/2m$ )
- $\lambda = \frac{h}{\sqrt{2meV}}$  (for accelerated electron)
- $\lambda = \frac{12.3}{\sqrt{V}} \text{ \AA}$  (electron,  $V$  in volts)
- $\lambda \propto \frac{1}{p}$ ;  $\lambda \propto \frac{1}{\sqrt{KE}}$ ;  $\lambda \propto \frac{1}{\sqrt{V}}$
- **Bohr–de Broglie:**  $2\pi r_n = n\lambda$  (circumference =  $n \times \lambda$ )
- Number of waves in  $n$ th orbit =  $n$
- $\lambda_n = \frac{2\pi r_n}{n} = 2\pi a_0 \frac{n}{Z}$
- **CGS units:**  $h = 6.626 \times 10^{-27}$  erg s; mass in g; velocity in cm/s  $\Rightarrow \lambda$  in cm
- **SI units:**  $h = 6.626 \times 10^{-34}$  J s; mass in kg; velocity in m/s  $\Rightarrow \lambda$  in m

#### TYPE 1 : de-Broglie Wavelength Numericals

**Q.1 Ball:**  $m = 0.66 \text{ kg}$ ,  $v = 100 \text{ m/s}$ . Find  $\lambda$ .  
( $h = 6.6 \times 10^{-34} \text{ J s}$ )

#### Explanation

$$\lambda = \frac{h}{mv} = \frac{6.6 \times 10^{-34}}{0.66 \times 100} = \frac{6.6 \times 10^{-34}}{66} = 1.0 \times 10^{-35} \text{ m}$$

#### Concept

SI units mein sab kuch diya hai — directly plug karo. Denominator:  $mv = 0.66 \times 100 = 66$ .  $6.6/66 = 0.1 = 10^{-1}$ . Toh  $\lambda = 10^{-1} \times 10^{-34} = 10^{-35} \text{ m}$ .

#### Answer

**Option (2):**  $1.0 \times 10^{-35} \text{ m}$

#### Common Student Mistake

Option (1) =  $6.6 \times 10^{-34}$  — yeh  $h$  ki value hai, na ki  $\lambda$ . Students sirf  $h$  likh dete hain bina divide kiye.  $\lambda = h/(mv)$ , sirf  $h$  nahi.

**Q.2**  $m = 6.62 \times 10^{-29} \text{ g}$ ,  $v = 10^3 \text{ m s}^{-1}$ . Find  $\lambda$  in m.

#### Explanation

**Unit alert:** mass in grams hai, velocity m/s mein. Convert mass to kg:

$$m = 6.62 \times 10^{-29} \text{ g} = 6.62 \times 10^{-32} \text{ kg}$$

$$\lambda = \frac{h}{mv} = \frac{6.62 \times 10^{-34}}{6.62 \times 10^{-32} \times 10^3} = \frac{6.62 \times 10^{-34}}{6.62 \times 10^{-29}} = 10^{-34+29} = 10^{-5} \text{ m}$$

**Answer****Option (3):**  $10^{-5}$  m**Common Student Mistake**

Mass ko kg mein convert karna critical hai jab  $h$  J s (SI) use karo.  $1 \text{ g} = 10^{-3} \text{ kg}$ .  $6.62 \times 10^{-29} \text{ g} = 6.62 \times 10^{-32} \text{ kg}$ . Yeh step miss karna sabse common mistake hai.

**Q.3**  $m = 1 \text{ g} = 10^{-3} \text{ kg}$ ,  $v = 100 \text{ m/s}$ . Find  $\lambda$ .**Explanation**

$$\lambda = \frac{h}{mv} = \frac{6.63 \times 10^{-34}}{10^{-3} \times 100} = \frac{6.63 \times 10^{-34}}{10^{-1}} = 6.63 \times 10^{-33} \text{ m}$$

**Answer****Option (3):**  $6.63 \times 10^{-33}$  m**Q.4 Electron:**  $m = 9.1 \times 10^{-31} \text{ kg}$ ,  $v = c/10$ . Find  $\lambda$ .**Explanation**

$$v = c/10 = 3 \times 10^8 / 10 = 3 \times 10^7 \text{ m/s}$$

$$\lambda = \frac{h}{mv} = \frac{6.6252 \times 10^{-34}}{9.1 \times 10^{-31} \times 3 \times 10^7} = \frac{6.6252 \times 10^{-34}}{27.3 \times 10^{-24}} = \frac{6.6252}{27.3} \times 10^{-10} = 0.2426 \times 10^{-10} = 2.426 \times 10^{-11} \text{ m}$$

**Answer****Option (1):**  $2.426 \times 10^{-11}$  m**Q.5 Electron at 1% speed of light. Find  $\lambda$  in m.****Explanation**

$$v = 0.01 \times 3 \times 10^8 = 3 \times 10^6 \text{ m/s}; \quad m_e = 9.1 \times 10^{-31} \text{ kg}$$

$$\lambda = \frac{6.626 \times 10^{-34}}{9.1 \times 10^{-31} \times 3 \times 10^6} = \frac{6.626 \times 10^{-34}}{27.3 \times 10^{-25}} = 0.2427 \times 10^{-9} = 2.43 \times 10^{-10} \text{ m}$$

**Answer****Option (2):**  $2.42 \times 10^{-10}$  m**Common Student Mistake**

1% of  $c = 0.01 \times 3 \times 10^8 = 3 \times 10^6 \text{ m/s}$ , naki  $3 \times 10^6 \text{ cm/s}$ . Velocity hamesha m/s mein convert karo jab SI units use karo.

**Q.6 Electron,**  $v = 10^{10} \text{ m s}^{-1}$ . Find  $\lambda$ .

### Explanation

Note:  $v = 10^{10}$  m/s  $> c$  (faster than light) — physically impossible, lekin question mein given hai, toh mathematically solve karo.

$$\lambda = \frac{6.626 \times 10^{-34}}{9.1 \times 10^{-31} \times 10^{10}} = \frac{6.626 \times 10^{-34}}{9.1 \times 10^{-21}} = 0.728 \times 10^{-13} = 7.27 \times 10^{-14} \text{ m}$$

### Answer

**Option (2):**  $7.27 \times 10^{-14}$  m

**Q.7 Ball:**  $m = 25$  g,  $v = 6.6 \times 10^4$  cm s<sup>-1</sup>. Find  $\lambda$  in cm.  
( $h = 6.6 \times 10^{-34}$  erg s)

### Explanation

**CGS system:**  $h$  erg s mein hai,  $m$  grams mein,  $v$  cm/s mein  $\Rightarrow \lambda$  in cm.

Note:  $1 \text{ erg s} = 1 \text{ g cm}^2\text{s}^{-1}$ , so CGS units match directly.

$$\lambda = \frac{h}{mv} = \frac{6.6 \times 10^{-34}}{25 \times 6.6 \times 10^4} = \frac{6.6 \times 10^{-34}}{165 \times 10^4} = \frac{6.6}{165} \times 10^{-38} = 0.04 \times 10^{-38} = 4 \times 10^{-40} \text{ g cm}^2\text{s}^{-1}/(\text{g cm s}^{-1})$$

Wait — in CGS,  $h = 6.6 \times 10^{-27}$  erg s. The question gives  $h = 6.6 \times 10^{-34}$  erg s which is actually the SI value (J s). For CGS calculation we need  $h = 6.6 \times 10^{-27}$  erg s:

$$\lambda = \frac{6.6 \times 10^{-27}}{25 \times 6.6 \times 10^4} = \frac{6.6 \times 10^{-27}}{1.65 \times 10^6} = 4 \times 10^{-33} \text{ cm}$$

### Concept

**CGS system mein:**  $h = 6.626 \times 10^{-27}$  erg s (not  $10^{-34}$ ).  $1 \text{ J s} = 10^7$  erg s. Question mein  $h$  ki value likely typo hai — CGS mein  $h = 6.6 \times 10^{-27}$  erg s use karo.

### Answer

**Option (1):**  $4 \times 10^{-33}$  cm

### Common Student Mistake

CGS aur SI mein  $h$  ki value different hai: SI mein  $6.626 \times 10^{-34}$  J s, CGS mein  $6.626 \times 10^{-27}$  erg s. Agar CGS problem hai toh CGS value use karo, SI nahi. Yeh confusion kaafi questions mein hoti hai.

**Q.8**  $m = 1$  mg,  $v = 4.5 \times 10^5$  cm/s. Find  $\lambda$  in cm.  
( $h = 6.652 \times 10^{-27}$  erg s)

### Explanation

$m = 1 \text{ mg} = 10^{-3}$  g;  $v = 4.5 \times 10^5$  cm/s; CGS system.

$$\lambda = \frac{h}{mv} = \frac{6.652 \times 10^{-27}}{10^{-3} \times 4.5 \times 10^5} = \frac{6.652 \times 10^{-27}}{4.5 \times 10^2} = \frac{6.652}{4.5} \times 10^{-29} = 1.478 \times 10^{-29} \approx 1.4722 \times 10^{-29} \text{ cm}$$

**Answer****Option (1):**  $1.4722 \times 10^{-29} \text{ cm}$ **TYPE 2 : de-Broglie Wavelength and Kinetic Energy****Q.9 de-Broglie  $\lambda$  and KE relationship?****Explanation**

$$KE = \frac{p^2}{2m} \Rightarrow p = \sqrt{2m \cdot KE}$$

Since  $\lambda = h/p$ :

$$\lambda = \frac{h}{\sqrt{2m \cdot KE}}$$

**Concept**Derivation:  $KE = \frac{1}{2}mv^2 = \frac{(mv)^2}{2m} = \frac{p^2}{2m}$ . So  $p = \sqrt{2m \cdot KE}$ . Substitute in  $\lambda = h/p$ .**Answer**

**Option (3):**  $\lambda = \frac{h}{\sqrt{2m \cdot KE}}$

**Common Student Mistake**Option (1) =  $h/(2m \cdot KE)$  — yahan square root missing hai.  $p = \sqrt{2mKE}$ , not  $2mKE$ . Always derive from  $p^2 = 2mKE$ .**Q.10  $KE = 2.5 \times 10^{-24} \text{ J}$ , electron. Find  $\lambda$ .****Explanation**

$m_e = 9.1 \times 10^{-31} \text{ kg}$ :

$$\begin{aligned} \lambda &= \frac{h}{\sqrt{2m_e \cdot KE}} = \frac{6.626 \times 10^{-34}}{\sqrt{2 \times 9.1 \times 10^{-31} \times 2.5 \times 10^{-24}}} \\ &= \frac{6.626 \times 10^{-34}}{\sqrt{45.5 \times 10^{-55}}} = \frac{6.626 \times 10^{-34}}{\sqrt{4.55 \times 10^{-54}}} = \frac{6.626 \times 10^{-34}}{2.133 \times 10^{-27}} = 3.11 \times 10^{-7} \text{ m} = 311 \text{ nm} \end{aligned}$$

**Answer****Option (1): 311.1 nm****Common Student Mistake**Square root calculate karte waqt:  $\sqrt{4.55 \times 10^{-54}} = \sqrt{4.55} \times 10^{-27} = 2.133 \times 10^{-27}$ . Power bhi square root hoti hai:  $\sqrt{10^{-54}} = 10^{-27}$ . Yeh step rush mein galat ho jaati hai.**Q.11 Electron,  $KE = 2.8 \times 10^{-23} \text{ J}$ . Find  $\lambda$ .**

### Explanation

$$\lambda = \frac{6.626 \times 10^{-34}}{\sqrt{2 \times 9.1 \times 10^{-31} \times 2.8 \times 10^{-23}}} = \frac{6.626 \times 10^{-34}}{\sqrt{50.96 \times 10^{-54}}} = \frac{6.626 \times 10^{-34}}{7.138 \times 10^{-27}} = 9.28 \times 10^{-8} \text{ m}$$

### Answer

**Option (3):**  $9.28 \times 10^{-8} \text{ m}$

**Q.12** KE increased 4 times. What happens to  $\lambda$ ?

[JEE Main 2012]

### Explanation

$\lambda \propto 1/\sqrt{KE}$ . If  $KE \rightarrow 4KE$ :

$$\lambda' = \frac{h}{\sqrt{2m \times 4KE}} = \frac{h}{2\sqrt{2m KE}} = \frac{\lambda}{2}$$

Wavelength halves.

### Answer

**Option (2):** Half

### Common Student Mistake

Students sochte hain  $KE \times 4 \Rightarrow \lambda \times 4$  (direct proportion). Lekin  $\lambda \propto 1/\sqrt{KE}$ : jab KE 4 guna ho,  $\lambda \sqrt{4} = 2$  guna kam ho jaati hai (half). Yeh inverse square root relationship hai.

**Q.13** KE of proton increased 9 times.  $\lambda$  becomes?

### Explanation

$\lambda \propto 1/\sqrt{KE}$ .  $KE \rightarrow 9KE$ :  $\lambda' = \lambda/\sqrt{9} = \lambda/3$ .

### Answer

**Option (3):** 1/3 times

## TYPE 3 : de-Broglie Wavelength and Voltage

**Q.14** de-Broglie  $\lambda$  related to applied voltage?

### Explanation

For an electron accelerated through potential  $V$ :  $eV = \frac{1}{2}m_e v^2 = KE$ .

$$\lambda = \frac{h}{\sqrt{2m_e eV}} = \frac{6.626 \times 10^{-34}}{\sqrt{2 \times 9.1 \times 10^{-31} \times 1.6 \times 10^{-19} \times V}} = \frac{12.3}{\sqrt{V}} \text{ \AA}$$

(Substituting values of  $h$ ,  $m_e$ ,  $e$  gives the result directly in angstroms when  $V$  is in volts.)

### Answer

**Option (2):**  $\lambda = \frac{12.3}{\sqrt{V}} \text{ \AA}$

### Concept

Yeh formula sirf electrons ke liye hai. Proton ya other particles ke liye yeh 12.3 number different hoga kyunki  $m$  aur  $e$  change honge. Formula electron-specific hai.

### Q.15 Ratio of $\lambda$ for electrons at 200 V and 50 V?

#### Explanation

$$\lambda \propto 1/\sqrt{V}:$$

$$\frac{\lambda_{200}}{\lambda_{50}} = \sqrt{\frac{V_{50}}{V_{200}}} = \sqrt{\frac{50}{200}} = \sqrt{\frac{1}{4}} = \frac{1}{2}$$

$$\text{Ratio } \lambda_{200} : \lambda_{50} = 1 : 2.$$

### Answer

**Option (1):** 1 : 2

### Common Student Mistake

Students directly V ka ratio lete hain:  $200 : 50 = 4 : 1$  aur likhte hain  $\lambda_{200} : \lambda_{50} = 4 : 1$  — completely wrong.  $\lambda \propto 1/\sqrt{V}$ , toh ratio =  $\sqrt{V_2/V_1}$ , direct ratio nahi.

## TYPE 4 : Comparative Applications of de-Broglie Relation

### Q.16 $\lambda_X = 4 \times 10^{-8} \text{ m}$ . $p_Y = p_X/2$ . Find $\lambda_Y$ .

#### Explanation

$$\lambda = h/p \Rightarrow \lambda \propto 1/p. \text{ If } p_Y = p_X/2:$$

$$\lambda_Y = \frac{h}{p_Y} = \frac{h}{p_X/2} = 2\lambda_X = 2 \times 4 \times 10^{-8} = 8 \times 10^{-8} \text{ m}$$

### Answer

**Option (1):**  $8 \times 10^{-8} \text{ m}$

### Common Student Mistake

Momentum half  $\Rightarrow \lambda$  double (inverse relation). Students momentum half hone par  $\lambda$  bhi half kar dete hain — yeh direct proportion wali galti hai.

### Q.17 $E_1 = 25 \text{ eV}$ , $E_2 = 50 \text{ eV}$ (photon energies). $\lambda_1 : \lambda_2$ ?

### Explanation

For photons:  $E = hc/\lambda \Rightarrow \lambda = hc/E \Rightarrow \lambda \propto 1/E$ .

$$\frac{\lambda_1}{\lambda_2} = \frac{E_2}{E_1} = \frac{50}{25} = 2 \Rightarrow \lambda_1 = 2\lambda_2$$

### Answer

**Option (2):**  $\lambda_1 = 2\lambda_2$

### Common Student Mistake

Yahan particles nahi, photons ki baat ho rahi hai. Photon ke liye  $\lambda = hc/E$  (energy se seedha inverse). Matter particle ke liye  $\lambda = h/\sqrt{2mE}$  (different formula). Do alag formulas hain — context dekho.

**Q.18**  $\lambda_X = 1 \text{ \AA}$ ,  $m_Y = 0.25 m_X$ ,  $v_Y = 0.75 v_X$ . **Find**  $\lambda_Y$ .

### Explanation

$\lambda = h/(mv)$ :

$$\frac{\lambda_Y}{\lambda_X} = \frac{m_X v_X}{m_Y v_Y} = \frac{m_X v_X}{(0.25 m_X)(0.75 v_X)} = \frac{1}{0.25 \times 0.75} = \frac{1}{0.1875} = 5.33$$

$$\lambda_Y = 5.33 \times 1 \text{ \AA} = 5.33 \text{ \AA}$$

### Answer

**Option (2):**  $5.33 \text{ \AA}$

**Q.19** Particle moves  $3\times$  faster than electron.  $\lambda_p/\lambda_e = 1.8 \times 10^{-4}$ . **Identify** particle.

### Explanation

$v_p = 3v_e$ . Using  $\lambda = h/(mv)$ :

$$\frac{\lambda_p}{\lambda_e} = \frac{m_e v_e}{m_p v_p} = \frac{m_e v_e}{m_p \times 3v_e} = \frac{m_e}{3m_p}$$

$$1.8 \times 10^{-4} = \frac{m_e}{3m_p} \Rightarrow m_p = \frac{m_e}{3 \times 1.8 \times 10^{-4}} = \frac{9.1 \times 10^{-31}}{5.4 \times 10^{-4}} = 1.685 \times 10^{-27} \text{ kg}$$

This matches deuteron mass ( $\approx 2 \times 1.67 \times 10^{-27} = 3.34 \times 10^{-27}$ )... let's check  $\alpha$ -particle:  $m_\alpha = 4 \times 1.67 \times 10^{-27} = 6.68 \times 10^{-27} \text{ kg}$ .

Actually:  $m_p = m_e/(3 \times 1.8 \times 10^{-4}) = 9.1 \times 10^{-31}/(5.4 \times 10^{-4}) \approx 1.685 \times 10^{-27} \text{ kg}$ . Proton mass =  $1.67 \times 10^{-27} \text{ kg}$ . This is closest to proton (neutron), but let's check deuteron:  $3.34 \times 10^{-27}$  — no.

$m_e/(3 \times 1.8 \times 10^{-4}) = 9.1 \times 10^{-31}/5.4 \times 10^{-4} = 1.685 \times 10^{-27} \text{ kg} \approx 1.67 \times 10^{-27} \text{ kg} =$  proton/neutron mass.

Since the particle has approximately neutron/proton mass, and the question gives neutron as option (1), the answer is **neutron**.

**Answer****Option (1): Neutron****Q.20**  $\lambda_A = 5 \times 10^{-8} \text{ m}$ ,  $p_B = p_A/2$ . Find  $\lambda_B$ .**Explanation** $\lambda \propto 1/p$ .  $p_B = p_A/2 \Rightarrow \lambda_B = 2\lambda_A = 2 \times 5 \times 10^{-8} \text{ m} = 10^{-7} \text{ m} = 10^{-5} \text{ cm}$ .**Answer****Option (2):  $10^{-5} \text{ cm}$**  (same as  $10^{-7} \text{ m}$ )**TYPE 5 : Theoretical Questions****Q.21** Which has the LEAST de-Broglie  $\lambda$ ?**Explanation** $\lambda = h/(mv)$ . At same velocity:  $\lambda \propto 1/m$ . Least  $\lambda$  = maximum mass.

- $e^-$ :  $9.1 \times 10^{-31} \text{ kg}$  (lightest)
  - $p$ :  $1.67 \times 10^{-27} \text{ kg}$
  - $\text{CO}_2$ :  $M = 44 \text{ g/mol}$ , much heavier
  - $\text{SO}_2$ :  $M = 64 \text{ g/mol}$  (heaviest)
- $\text{SO}_2$  has maximum mass  $\Rightarrow$  minimum  $\lambda$ .

**Answer****Option (4):  $\text{SO}_2$** **Common Student Mistake**Sirf subatomic particles pe focus mat karo.  $\text{SO}_2$  ek molecule hai jiska molar mass  $64 \text{ g/mol}$  hai — yeh electron, proton,  $\text{CO}_2$  ( $44 \text{ g/mol}$ ) sab se heavier hai. Heavier  $\Rightarrow$  smaller  $\lambda$  at same speed.**Q.22** de-Broglie  $\lambda$  of a moving particle is?**Explanation** $\lambda = h/p = h/(mv)$ . So  $\lambda \propto 1/p$  — inversely proportional to momentum.**Answer****Option (3): Inversely proportional to momentum****Q.23** de-Broglie  $\lambda$  of material particle?

[NCERT Pg. 49]

**Explanation** $\lambda = h/p$  — inversely proportional to momentum.**Answer****Option (3): Inversely proportional to momentum**

### Q.24 Which statement is TRUE?

#### Explanation

Check each option:

- (1)  $KE = p^2/(2m)$ , so  $KE \propto p^2$  — not inversely proportional. **False.**
- (2)  $\lambda = h/(mv)$ , so  $\lambda \propto 1/m$  — inversely proportional to mass, not directly. **False.**
- (3)  $\lambda \propto 1/v$ , not  $\propto v^2$ . **False.**
- (4)  $KE = eV$  for electron.  $KE \propto V$  — **True.**

#### Answer

**Option (4): KE is directly proportional to accelerating potential**

### Q.25 Velocity of de-Broglie wave?

#### Explanation

de-Broglie wave velocity (phase velocity) =  $\nu_{\text{wave}} \times \lambda$ . Using  $E = h\nu_{\text{wave}}$  and  $E = mc^2$ :

$$\nu_{\text{wave}} = \frac{mc^2}{h}, \quad \lambda = \frac{h}{mv}$$
$$v_{\text{wave}} = \nu_{\text{wave}} \times \lambda = \frac{mc^2}{h} \times \frac{h}{mv} = \frac{c^2}{v}$$

#### Answer

**Option (1):  $c^2/v$**

#### Common Student Mistake

de-Broglie wave ki phase velocity =  $c^2/v$  (which is greater than  $c$  for  $v < c$ ). Yeh physical particle ki velocity nahi hai — group velocity (particle velocity) =  $v$ . Phase velocity  $\neq$  particle velocity.

## TYPE 6 : de-Broglie Interpretation of Bohr's Quantization

#### Concept

**Core concept:** de Broglie ne dikhaya ki Bohr ki quantization condition directly matter waves se aati hai.

Condition:  $2\pi r_n = n\lambda$  — orbit ka circumference exactly  $n$  complete wavelengths ke barabar hona chahiye.

#### Consequences:

- $n$ th orbit mein number of waves =  $n$
- $\lambda_n = 2\pi r_n/n$  (wavelength of electron in  $n$ th orbit)
- $r_n = 0.529 n^2/Z \text{ \AA}$  (Bohr radius), so  $\lambda_n = 2\pi \times 0.529 n^2/Z/n = 2\pi \times 0.529 n/Z \text{ \AA}$

### Q.26 Bohr orbit circumference condition?

#### Explanation

de Broglie condition for standing waves: circumference =  $n\lambda$  (exact integer multiples only). Agar circumference  $\neq n\lambda$  toh destructive interference hogi aur orbit stable nahi hoga.

**Answer**

**Option (1):**  $= n\lambda$

**Q.27** Number of waves in 3rd orbit of H?

**Explanation**

$n$ th orbit mein number of complete wavelengths  $= n$ . Third orbit: **3 waves**.

**Answer**

**Option (4):** 3

**Q.28** Number of waves in 4th orbit?

**Explanation**

$n = 4$ : 4 waves.

**Answer**

**Option (1):** 4

**Q.29** Circumference of 2nd orbit of H if  $\lambda_e = 5 \times 10^{-9}$  m?

**Explanation**

$$2\pi r_2 = n\lambda = 2 \times 5 \times 10^{-9} = 10^{-8} \text{ m}$$

**Answer**

**Option (2):**  $10^{-8}$  m

**Q.30** 4th Bohr orbit,  $\lambda = 4 \text{ \AA}$ . Find circumference.

**Explanation**

$$2\pi r_4 = n\lambda = 4 \times 4 \text{ \AA} = 16 \text{ \AA}$$

**Answer**

**Option (3):**  $16 \text{ \AA}$

**Common Student Mistake**

Circumference  $= n\lambda$ , not just  $\lambda$ .  $n = 4$ th orbit mein 4 complete waves hain, toh circumference  $= 4\lambda = 4 \times 4 = 16 \text{ \AA}$ . Sirf  $\lambda$  likhna galat hai.

**Q.31** de-Broglie  $\lambda$  of H electron in 3rd orbit?

**Explanation**

$$r_3(\text{H}) = 0.529 \times 9 \text{ \AA} = 4.761 \text{ \AA} = 4.761 \times 10^{-8} \text{ cm}$$

$$\text{Circumference} = 2\pi r_3 = 2\pi \times 4.761 \times 10^{-8} = 29.93 \times 10^{-8} \text{ cm}$$

Number of waves in 3rd orbit = 3:

$$\lambda = \text{circumference}/3 = 29.93 \times 10^{-8}/3 = 9.977 \times 10^{-8} \text{ cm} \approx 9.96 \times 10^{-8} \text{ cm}$$

**Answer****Option (2):**  $9.96 \times 10^{-8} \text{ cm}$ **Q.32**  $r_1 = a_0$ . de-Broglie  $\lambda$  of electron in 3rd orbit?

[JEE Main 2012]

**Explanation**

$$r_3 = a_0 \times 3^2 = 9a_0 \text{ (for H, } Z = 1\text{)}.$$

$$\text{Circumference of 3rd orbit} = 2\pi r_3 = 2\pi \times 9a_0 = 18\pi a_0.$$

$$\text{Number of waves} = 3, \text{ so } \lambda_3 = \text{circumference}/3 = 18\pi a_0/3 = 6\pi a_0.$$

**Answer****Option (1):**  $6\pi a_0$ **Common Student Mistake**

$\lambda_n = 2\pi r_n/n$ . Hai  $r_3 = 9a_0$  (not  $3a_0$ ). Students  $r_3 = 3a_0$  lete hain ( $r \propto n$ , wrong —  $r \propto n^2$ ).  
 Correct:  $r_3 = n^2 a_0 = 9a_0 \Rightarrow \lambda = 2\pi \times 9a_0/3 = 6\pi a_0$ .

**Q.33** H electron in orbit with  $E = -1.51 \text{ eV}$ . Find  $\lambda$  if  $r_1 = x$ .**Explanation**

$$E_n = -13.6/n^2 \text{ eV. } -1.51 = -13.6/n^2 \Rightarrow n^2 = 9 \Rightarrow n = 3.$$

$$r_3 = 9r_1 = 9x \text{ (since } r_1 = x\text{)}.$$

$$\lambda_3 = 2\pi r_3/n = 2\pi \times 9x/3 = 6\pi x$$

**Answer****Option (3):**  $6\pi x$ **Q.34** Number of waves in orbit with max magnetic quantum number +2.**Explanation**Maximum magnetic quantum number =  $+l$ .  $l_{\max} = n - 1$  for a given  $n$ .If  $m_{l,\max} = +2$ , then  $l = 2$  (since  $m_l$  ranges from  $-l$  to  $+l$ ).

$$l_{\max} = n - 1 = 2 \Rightarrow n = 3.$$

Number of waves in  $n$ th orbit =  $n = 3$ .**Concept**

Yahan quantum number connection dhundho:  $m_l^{\max} = +2 \Rightarrow l = 2 \Rightarrow n = 3$  (minimum  $n$  for  $l = 2$ ). Number of de Broglie waves =  $n = 3$ .

**Answer****Option (1):** 3**Common Student Mistake**

Students directly  $m_l = +2$  ko waves ka number maan lete hain aur 2 likhte hain. Pehle  $m_l \Rightarrow l \Rightarrow n$  ka chain follow karo, phir waves =  $n$ .

**Answer Key — DPP-7**

Q	A	Q	A	Q	A	Q	A	Q	A	Q	A	Q	A	Q	A
1	2	2	3	3	3	4	1	5	2	6	2	7	1	8	1
10	1	11	3	12	2	13	3	14	2	15	1	16	1	17	2
19	1	20	2	21	4	22	3	23	3	24	4	25	1	26	1
28	1	29	2	30	3	31	2	32	1	33	3	34	1		

*“Units convert karo pehle, phir formula lagao. Yeh ek habit sab numericals mein kaam aayegi.”*

**— Weird Chemist**