

Concentration-3

Some Basic concepts of Chemistry-6

1. 8 g of NaOH is dissolved in 18 g of H₂O. Mole fraction of NaOH in solution and molality (mol kg⁻¹) are [JEE(Main) 2019].

Explanation (simple words): 8 g NaOH ⇒ moles solute; 18 g water ⇒ 1 mol solvent.

Approach: $x_{\text{NaOH}} = \frac{n_{\text{NaOH}}}{n_{\text{NaOH}} + n_{\text{H}_2\text{O}}}$; $m = \frac{n_{\text{NaOH}}}{m_{\text{solvent}}(\text{kg})}$.

Steps:

$$n_{\text{NaOH}} = \frac{8}{40} = 0.200 \text{ mol}, \quad n_{\text{H}_2\text{O}} = \frac{18}{18} = 1.000 \text{ mol}$$
$$x_{\text{NaOH}} = \frac{0.2}{0.2 + 1.0} = \boxed{0.167} \quad (= 1/6)$$
$$m = \frac{0.200}{0.018} = \boxed{11.11 \text{ m}}$$

Why this formula? Mole fraction uses moles; molality uses *mass of solvent* (kg).

Similar practice (with answer): 4 g KOH in 36 g water: $n = 0.0711$, $x = 0.0711/(0.0711 + 2) = \boxed{0.0345}$; $m = 0.0711/0.036 = \boxed{1.97 \text{ m}}$.

2. Sugar (C₁₂H₂₂O₁₁) mass required to prepare 2.0 L of 0.10 M solution [JEE(Main) 2019].

Explanation (simple words): Moles needed = MV ; mass = nM .

Steps:

$$n = 0.10 \times 2.0 = 0.20 \text{ mol}, \quad M = 342 \text{ g mol}^{-1}$$
$$m = 0.20 \times 342 = \boxed{68.4 \text{ g}}$$

Similar practice (with answer): 0.25 M, 1.5 L solution needs 0.375 mol ⇒ mass = $0.375 \times 342 = \boxed{128.25 \text{ g}}$.

3. A solution contains 92 g of Na⁺ ions per kg of water. Molality of Na⁺ in solution is [JEE(Main) 2019].

Approach: $n(\text{Na}^+) = 92/23 = 4 \text{ mol}$; $m = \frac{n}{1 \text{ kg}}$.

Answer: $\boxed{4.0 \text{ m}}$.

Similar practice (with answer): 36.5 g Cl⁻ per kg water ⇒ $n = 1.03 \text{ mol}$ ⇒ $m = \boxed{1.03 \text{ m}}$.

4. Molarity after mixing 750 mL of 0.5 M HCl with 250 mL of 2.0 M HCl [JEE(Main) 2013].

Approach: $M = \frac{M_1V_1 + M_2V_2}{V_1 + V_2}$ with volumes in L.

Steps:

$$M = \frac{0.5 \times 0.750 + 2.0 \times 0.250}{1.000} = \frac{0.375 + 0.500}{1.000} = \boxed{0.875 \text{ M}}$$

Similar practice (with answer): 200 mL 1 M + 300 mL 0.4 M $\Rightarrow M = \frac{0.2 + 0.12}{0.5} = \boxed{0.64 \text{ M}}$.

5. The mole fraction of solvent in an aqueous solution is 0.80. Find the molality.

Explanation (simple words): Choose an easy basis: take 4 mol water and 1 mol solute (gives $x_{\text{solvent}} = 4/(4 + 1) = 0.8$).

Steps:

$$m = \frac{1 \text{ mol}}{(4 \times 18) \text{ g}/1000} = \frac{1}{0.072} = \boxed{13.89 \text{ m}}$$

Why this formula? Molality uses *mass of solvent*, independent of temperature.

Similar practice (with answer): If $x_{\text{solvent}} = 0.9$, take 9 mol water and 1 mol solute: $m = 1/(9 \times 18/1000) = \boxed{6.17 \text{ m}}$.

6. Molality of 20% (w/w) aqueous solution of KI (M=166 g mol⁻¹).

Explanation (simple words): In 100 g solution: 20 g KI, 80 g water.

Steps:

$$n_{\text{KI}} = \frac{20}{166} = 0.1205 \text{ mol}, \quad m = \frac{0.1205}{0.080} = \boxed{1.51 \text{ m}}$$

Similar practice (with answer): 10% (w/w) KI: $n = 10/166 = 0.0602$, $m = 0.0602/0.090 = \boxed{0.669 \text{ m}}$.

7. Dissolving 120 g urea (M=60) in 1000 g water gives a solution of density 1.15 g mL⁻¹. Find molarity [2011].

Steps:

$$n = \frac{120}{60} = 2.00 \text{ mol}, \quad m_{\text{soln}} = 1000 + 120 = 1120 \text{ g}$$
$$V = \frac{1120}{1.15} = 0.9739 \text{ L}, \quad M = \frac{2.00}{0.9739} = \boxed{2.05 \text{ M}}$$

Similar practice (with answer): 60 g urea in 500 g water, $\rho = 1.10 \text{ g mL}^{-1}$: $n = 1$, $V = 560/1.10 = 0.509 \text{ L} \Rightarrow M = \boxed{1.97 \text{ M}}$.

8. Which mode of expressing concentration is temperature independent?

Answer: $\boxed{\text{Molality}}$ (mass based).

Similar practice (with answer): Mass% or mole fraction are also T -independent.

9. A molal solution contains one mole of solute in —

Answer: $\boxed{1000 \text{ g of solvent}}$.

Similar practice (with answer): True/False: 1 m means 1 mol per litre of solution. $\rightarrow \boxed{\text{False}}$.

10. A syrup of mass 214.2 g contains 34.2 g sugar ($C_{12}H_{22}O_{11}$). Calculate (i) molarity and (ii) mole fraction of sugar. Given density = 1.84 g mL^{-1} .

Explanation (simple words): Moles sugar = $34.2/342 = 0.100 \text{ mol}$. Volume = m/ρ .

Steps:

$$V = \frac{214.2}{1.84} = 0.1164 \text{ L}$$

$$M = \frac{0.100}{0.1164} = \boxed{0.859 \text{ M}}$$

$$n_{\text{water}} = \frac{214.2 - 34.2}{18} = \frac{180.0}{18} = 10.0 \text{ mol}$$

$$x_{\text{sugar}} = \frac{0.100}{0.100 + 10.0} = \boxed{9.90 \times 10^{-3}}$$

Why this formula? Molarity uses litres of *solution*; mole fraction uses moles of all components.

Similar practice (with answer): If the density were 1.50 g mL^{-1} : $V = 0.1428 \text{ L} \Rightarrow M = \boxed{0.700 \text{ M}}$;

x unchanged = $\boxed{9.90 \times 10^{-3}}$.

11. Molality of 1.0 L of 37% (w/v) H_2SO_4 (density 1.84 g mL^{-1}).

Explanation (simple words): 37% (w/v) \Rightarrow 37 g acid per 100 mL solution \Rightarrow in 1 L, 370 g H_2SO_4 . Solution mass = 1840 g \Rightarrow solvent mass = $1840 - 370$.

Steps:

$$n_{\text{acid}} = \frac{370}{98} = 3.7755 \text{ mol}, \quad m_{\text{solvent}} = 1470 \text{ g} = 1.470 \text{ kg}$$

$$m = \frac{3.7755}{1.470} = \boxed{2.57 \text{ m}}$$

Similar practice (with answer): For 10% (w/v), $\rho = 1.10$: 100 g acid in 1 L, $m_{\text{solvent}} = 1100 - 100 = 1000 \text{ g}$, $m = \boxed{1.02 \text{ m}}$.

12. $8.0575 \times 10^{-2} \text{ kg}$ of Glauber's salt ($Na_2SO_4 \cdot 10H_2O$) is dissolved to obtain 1 dm^3 of solution with density 1077.2 kg m^{-3} . Calculate (i) molarity, (ii) molality, (iii) mole fraction of Na_2SO_4 .

Explanation (simple words): Molar mass($Na_2SO_4 \cdot 10H_2O$) = 322.0 g mol^{-1} ; anhydrous Na_2SO_4 = 142.0 g mol^{-1} . Water of crystallisation becomes part of solvent.

Steps:

$$m_{\text{salt}} = 80.575 \text{ g}, \quad n(Na_2SO_4) = \frac{80.575}{322.0} = \boxed{0.250 \text{ mol}}$$

$$(i) \quad M = \frac{0.250}{1.000} = \boxed{0.250 \text{ M}}$$

$$m_{\text{solution}} = 1077.2 \text{ g}; \quad m_{\text{solvent}} = m_{\text{solution}} - m_{\text{anhydrous}}$$

$$m_{\text{anhydrous}} = 0.250 \times 142.0 = 35.5 \text{ g}$$

$$m_{\text{solvent}} = 1077.2 - 35.5 = 1041.7 \text{ g} = 1.0417 \text{ kg}$$

$$(ii) \quad m = \frac{0.250}{1.0417} = \boxed{0.240 \text{ m}}$$

$$n_{\text{water}} = \frac{1041.7}{18} = 57.87 \text{ mol}$$

$$(iii) \quad x_{Na_2SO_4} = \frac{0.250}{0.250 + 57.87} = \boxed{4.30 \times 10^{-3}}$$

Why this formula? For hydrated salts, the water of crystallisation contributes to the solvent after dissolution.

Similar practice (with answer): If 161 g of $\text{Na}_2\text{SO}_4 \cdot 10\text{H}_2\text{O}$ were used (0.5 mol): $M = \boxed{0.50 \text{ M}}$, $m \approx \boxed{0.47 \text{ m}}$, $x \approx \boxed{8.6 \times 10^{-3}}$.

13. A 3 M $\text{Na}_2\text{S}_2\text{O}_3$ solution has density 1.25 g mL⁻¹. Calculate (i) % by weight of solute, (ii) mole fraction of solute, (iii) molalities of Na^+ and $\text{S}_2\text{O}_3^{2-}$.

Explanation (simple words): In 1 L: $n = 3$ mol; mass solute = $3 \times 158 = 474$ g; mass solution = 1250 g; solvent mass = 776 g.

Steps:

$$\begin{aligned} \text{(i) } \%w/w &= \frac{474}{1250} \times 100 = \boxed{37.9\%} \\ \text{(ii) } n_{\text{water}} &= \frac{776}{18} = 43.11 \text{ mol}, \quad x_{\text{solute}} = \frac{3}{3 + 43.11} = \boxed{0.0650} \\ \text{(iii) } m_{\text{Na}^+} &= \frac{2 \times 3}{0.776} = \boxed{7.73 \text{ m}}, \quad m_{\text{S}_2\text{O}_3^{2-}} = \frac{3}{0.776} = \boxed{3.87 \text{ m}} \end{aligned}$$

Similar practice (with answer): For a 2 M solution with $\rho = 1.20$: $\%w/w = \boxed{26.3\%}$, $x_{\text{solute}} \approx \boxed{0.043}$, $m_{\text{Na}^+} \approx \boxed{4.76 \text{ m}}$.

14. 100 mL of 0.50 M acetic acid is shaken with 1 g charcoal; final concentration is 0.49 M. If charcoal surface area is $3.01 \times 10^2 \text{ m}^2$, find area occupied by one acetic acid molecule on surface.

Explanation (simple words): Adsorbed moles = $\Delta(MV)$; divide surface area by number of molecules.

Steps:

$$\begin{aligned} n_{\text{ads}} &= (0.50 - 0.49) \times 0.100 = 1.0 \times 10^{-3} \text{ mol} \\ N &= nN_A = 1.0 \times 10^{-3} \times 6.022 \times 10^{23} = 6.022 \times 10^{20} \\ A_{\text{per molecule}} &= \frac{301 \text{ m}^2}{6.022 \times 10^{20}} = \boxed{5.0 \times 10^{-19} \text{ m}^2/\text{molecule}} \end{aligned}$$

Similar practice (with answer): If $\Delta c = 0.02 \text{ M}$ (same V and area): $n = 2 \times 10^{-3} \text{ mol} \Rightarrow A \approx \boxed{2.5 \times 10^{-19} \text{ m}^2}$.

15. A solution has $x_{\text{solute}} = 0.10$. At 298 K, its molarity equals its molality. Density = 2.90 g cm⁻³. Find $\frac{M_{\text{solute}}}{M_{\text{solvent}}}$.

Explanation (simple words): Let n_s moles solute, $n_w = 9n_s$ moles solvent (from $x = 0.1$). In 1 L solution, mass = $\rho V = 2900$ g.

Steps:

$$\begin{aligned} M = m &\Rightarrow n_s = \frac{1000}{9M_w} \\ 2900 &= n_s(M_s + 9M_w) = \frac{1000}{9M_w}(M_s + 9M_w) \\ \Rightarrow M_s &= (26.1 - 9)M_w = \boxed{17.1 M_w} \end{aligned}$$

Similar practice (with answer): If $\rho = 1.45 \text{ g cm}^{-3}$ (same x), ratio becomes $M_s = (13.05-9)M_w = \boxed{4.05 M_w}$.

16. A compound (M=80) is in a solvent of density 0.40 g mL^{-1} . Assuming solution volume \approx solvent volume, find molarity of a 3.2 m solution.

Explanation (simple words): Take 1 kg solvent: $n = 3.2 \text{ mol solute}$. Volume = m/ρ .

Steps:

$$V_{\text{solvent}} = \frac{1000 \text{ g}}{0.40} = 2500 \text{ mL} = 2.50 \text{ L}$$
$$M = \frac{n}{V} = \frac{3.2}{2.50} = \boxed{1.28 \text{ M}}$$

Similar practice (with answer): For a 2.0 m solution in same solvent: $M = 2.0/2.50 = \boxed{0.80 \text{ M}}$.
